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THE MATHEMATICAL

ASSOCIATION OF VICTORIA

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• Why?



#### Proficiencies

- Making reasonable estimates
- Calculate answers efficiently
- Recognise robust ways of answering questions
- Choose appropriate methods and approximations
- Recall definitions and use facts
- Can manipulate expressions and equations to find solutions
- Use mathematics to represent unfamiliar or meaningful situations
- Design investigations and plan their approaches
- Apply their existing strategies to seek solutions
- Verify that their answers are reasonable



- Explain their thinking
- Deduce and justify strategies used and conclusions reached
- Adapt the known to the unknown
- Transfer learning from one context to another
- Prove that something is true or false
  - Make inferences about data or the likelihood of events

Compare and contrast related ideas and explain their choices

#### Connect related ideas

- Represent concepts in different ways
- Identify commonalities and differences between aspects of content
- Describe their thinking mathematically
- Interpret mathematical information

## Toothpick puzzles – Farmers problem

Two farmers have land this shape.

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- (i) The first farmer wants to divide the land evenly among her 3 sons. Add 4 toothpicks to form 3 blocks of land of equal size and shape
- (ii) The second farmer wants to divide her land evenly amongst her 4 daughters.
  Use 8 toothpicks to form 4 blocks of land of equal size and identical shape.

#### Toothpick puzzles- Farmers dilemma Solution (i)





Two farmers have land this shape.

 (i) The first farmer wants to divide the land evenly among her 3 sons. Add 4 toothpicks to form 3 blocks of land of equal size and shape
 Possible solution showing 4 toothpicks to add

# Toothpick puzzles – Farmers problem



Two farmers have land this shape. (ii) The second farmer wants to divide her land evenly amongst her 4 daughters. Use 8 toothpicks to form 4 blocks of land of equal size and identical shape.

# Toothpick puzzles- Farmers dilema (solution (ii))





Two farmers have land this shape. (ii) The second farmer wants to divide her land evenly amongst her 4 daughters. Use 8 toothpicks to form 4 blocks of land of equal size and identical shape.

Possible solution showing 8 toothpicks to add

#### Warm Up Smorgasboard



- You will be assigned 4 different Warm Ups
- 1) Problem of the year
- 2) The 4 Four 4's
- 3) Quarter the Cross
- 4) One hole punches

Each table group will rotate through all 4 activities – 10 mins per activity

## Problem of the year - 2019



- Using the 2019 digits, i.e. 2, 0, 1, 9
- Can you make up all the numbers from 1 10, using the operations

+, - , ×, ÷,

and the power of 0 (use this as a last option)

• Complete on the worksheet provided

#### Problem of the year - 2019



2019	
1 =	
2 =	
3 =	$9 \div (2+1) + 0$
4 =	
5 =	
6 =	
7 =	
8 =	
9 =	
10 =	





 Write the whole numbers from 0 – 20 as calculations, each using exactly four of the number 4 and as many of the operations

as required.

e.g. 16 = 4+ 4+ 4 + 4

Six of the whole numbers from  $0 \rightarrow 20$  are not possible, which numbers are they?





• Is there one other function or operation you can use which makes ALL 20 numbers possible?

<u>https://blogs.adelaide.edu.au/maths-learning/category/one-hundred-factorial/</u> <u>@DavidKButlerUoA</u>

#### Quarter the cross



Colour in one quarter of this cross.

You have to be sure it's exactly a quarter.



#### Quarter the Cross













• More solutions tweet

#QuarterTheCross

# One-hole punch problems



- These are One-Hole Punch puzzles.
- To complete a puzzle, take a square of paper, fold it using as many folds as needed so that if you punch one hole and unfold it, you will match one of the puzzles.
- Complete the following puzzles in any order.
- Be prepared to discuss your strategies with others.



#### Some reflections



- How will you introduce these activities to your students?
- What information if any? about strategies will you provide?
- How would allowing students to work in pairs be different than working individually?
- What discussion can take place to help consolidate the learning?
- How might this be helpful before you give the next set of puzzles?
- What will you do if students give up quickly?
- What enabling prompts will you provide?





Graphs represent supermarket, library, café, gym. All in Preston. Think, pair share. Match the graph with the venue. Discuss with partner.







# Did you change your mind after discussing with partner?SOLUTIONS:



#### Some reflections



- What made these activities good?
- Which proficiencies are being addressed?





• Multiply

#### 111 111 111 by 111 111 111

#### 111 111 111 x 111 111 111

What is your result?

#### A final problem





#### 12 345 678 987 654 321





- The MAV would appreciate your feedback. Please take a couple of minutes to complete the following online survey.
- Friday 6 December 2019
- <u>https://www.surveymonkey.com/r/MAV190612</u>